

Programs as Data 8

A stack machine for micro-C; compiling micro-C to stack machine code

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Monday 2012-10-08



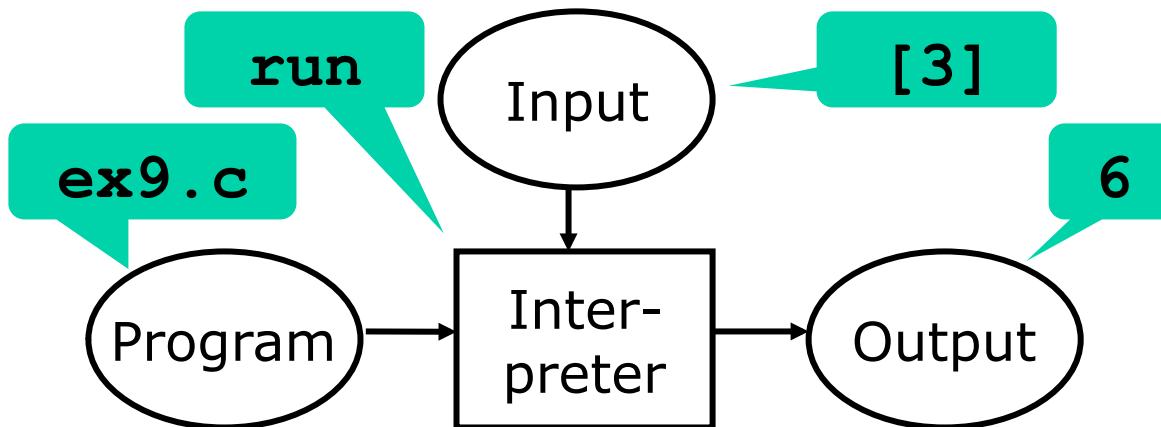
Today

- Stack machine, target for micro-C compiler
 - Stack machine state
 - Instruction set
 - Implementations in Java and C
- Compiling micro-C to stack machine code

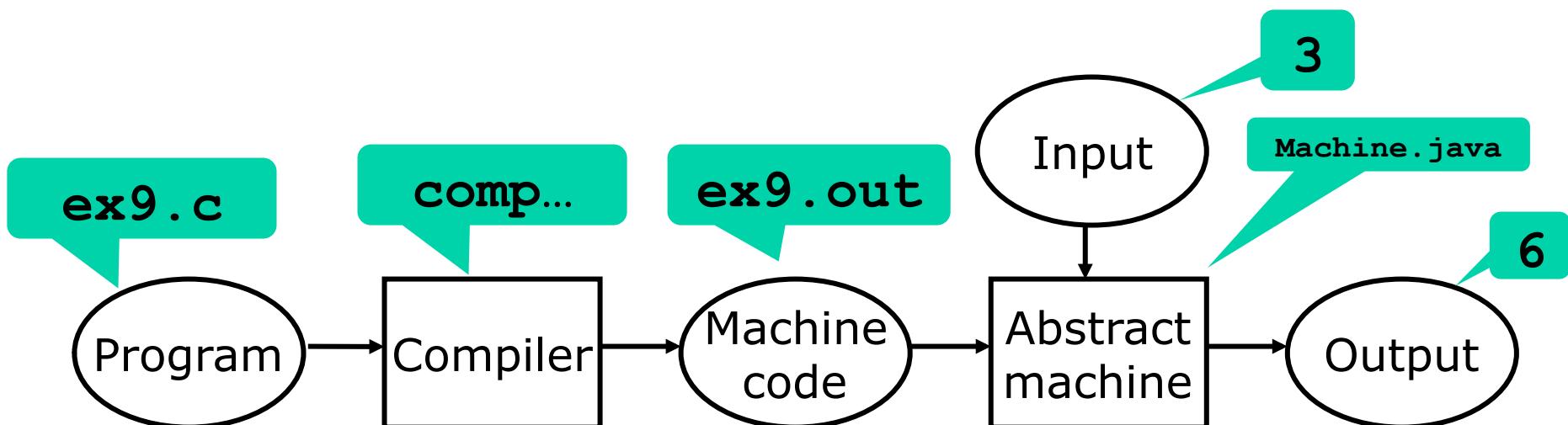


Interpretation and compilation

- Interpretation = one-stage execution/evaluation:



- Compilation = two-stage execution/evaluation:



Stack machine state transitions

Instruction	Stack before	Stack after	Effect
0 CSTI i	s	$\Rightarrow s, i$	Push constant i
1 ADD	s, i_1, i_2	$\Rightarrow s, (i_1 + i_2)$	Add
2 SUB	s, i_1, i_2	$\Rightarrow s, (i_1 - i_2)$	Subtract
3 MUL	s, i_1, i_2	$\Rightarrow s, (i_1 * i_2)$	Multiply
4 DIV	s, i_1, i_2	$\Rightarrow s, (i_1 / i_2)$	Divide
5 MOD	s, i_1, i_2	$\Rightarrow s, (i_1 \% i_2)$	Modulo
6 EQ	s, i_1, i_2	$\Rightarrow s, (i_1 = i_2)$	Equality (0 or 1)
7 LT	s, i_1, i_2	$\Rightarrow s, (i_1 < i_2)$	Less-than (0 or 1)
8 NOT	s, v	$\Rightarrow s, !v$	Negation (0 or 1)
9 DUP	s, v	$\Rightarrow s, v, v$	Duplicate
10 SWAP	s, v_1, v_2	$\Rightarrow s, v_2, v_1$	Swap
11 LDI	s, i	$\Rightarrow s, s[i]$	Load indirect
12 STI	s, i, v	$\Rightarrow s, v$	Store indirect $s[i] = v$
13 GETBP	s	$\Rightarrow s, bp$	Load base ptr bp
14 GETSP	s	$\Rightarrow s, sp$	Load stack ptr sp
15 INCSP m	s	$\Rightarrow s, v_1, \dots, v_m$	Grow stack ($m \geq 0$)
15 INCSP m	s, v_1, \dots, v_{-m}	$\Rightarrow s$	Shrink stack ($m < 0$)
16 GOTO a	s	$\Rightarrow s$	Jump to a
17 IFZERO a	s, v	$\Rightarrow s$	Jump to a if $v = 0$
18 IFNZRO a	s, v	$\Rightarrow s$	Jump to a if $v \neq 0$
19 CALL m a	s, v_1, \dots, v_m	$\Rightarrow s, r, bp, v_1, \dots, v_m$	Call function at a
20 TCALL m n a	$s, r, b, u_1, \dots, u_n, v_1, \dots, v_m$	$\Rightarrow s, r, b, v_1, \dots, v_m$	Tailcall function at a
21 RET m	$s, r, b, v_1, \dots, v_m, v$	$\Rightarrow s, v$	Return $bp = b, pc = r$
22 PRINTI	s, v	$\Rightarrow s, v$	Print integer v
23 PRINTC	s, v	$\Rightarrow s, v$	Print character v
24 LDARGS	s	$\Rightarrow s, i_1, \dots, i_n$	Command line args
25 STOP	s	$\Rightarrow \underline{\hspace{2cm}}$	Halt the machine

Example stack machine program

- A simple program, file prog1:

```
0 20000000 16 7 0 1 2 9 18 4 25
```

Numeric
code

```
0 20000000  
16 7  
0 1  
2  
9  
18 4  
25
```

```
0: CSTI 20000000  
2: GOTO 7  
4: CSTI 1  
6: SUB  
7: DUP  
8: IFNZRO 4  
10: STOP
```

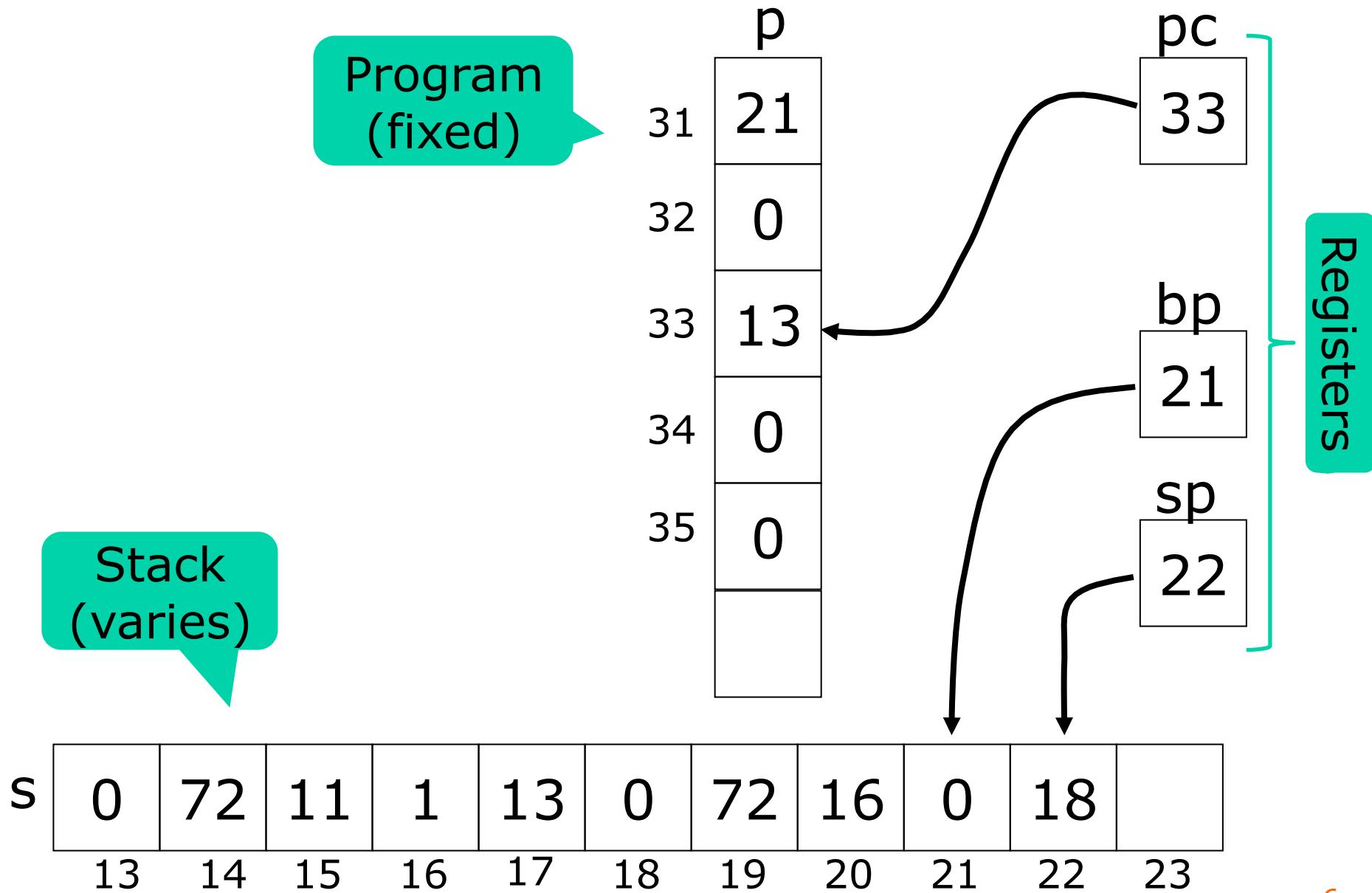
Symbolic
code

- Running the code in file prog1:

```
C:>java Machine prog1  
Ran 0.641 seconds
```



Machine state: p, pc, s, sp, bp



Stack machine for micro-C

- Runtime state:
 - Program **p**, holds the instructions
 - Program counter **pc**, points to next instruction
 - Stack **s**, holds variables and intermediate results
 - Stack pointer **sp**, points to top of stack
 - Base pointer **bp**, points to first local variable in top stack frame
- Structure of the stack
 - Bottom: Global variables
 - One stack frame for each active method



Implementations of the micro-C abstract machine

- File Machine.java: An implementation of the abstract machine as a Java program
- File machine.c: An implementation of the abstract machine as a C program
- File Machine.fs: A definition of the instruction set for use in the compiler Comp.fs
- The instruction numbers in Machine.fs agree with Machine.java and machine.c



Stack machine instruction execution

```
for (;;) {
    switch (p[pc++]) {
        case CSTI:
            s[sp+1] = p[pc++]; sp++; break;
        case ADD:
            s[sp-1] = s[sp-1] + s[sp]; sp--; break;
        case EQ:
            s[sp-1] = (s[sp-1] == s[sp] ? 1 : 0); sp--; break;
        case DUP:
            s[sp+1] = s[sp]; sp++; break;
        case LDI:
            s[sp] = s[s[sp]]; break;
        case GOTO:
            pc = p[pc]; break;
        case IFZERO:
            pc = (s[sp--] == 0 ? p[pc] : pc+1); break;
        case ...
        case STOP:
            return sp;
    ...
}
```

Java or C
or C#

Structure of the micro-C stack

- Computing factorial with MicroC/ex9.c

```
void main(int i) {
    int r;
    fac(i, &r);
    print r;
}

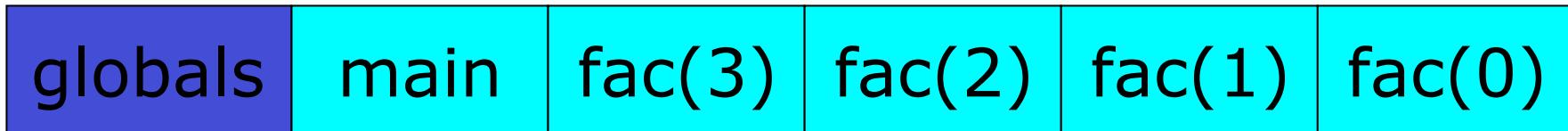
void fac(int n, int *res) {
    if (n == 0)
        *res = 1;
    else {
        int tmp;
        fac(n-1, &tmp);
        *res = tmp * n;
    }
}
```

- **n** is input parameter
- **res** is output parameter, a pointer to where to put the result
- **tmp** holds the result of the recursive call
- **&tmp** gets the pointer to **tmp**

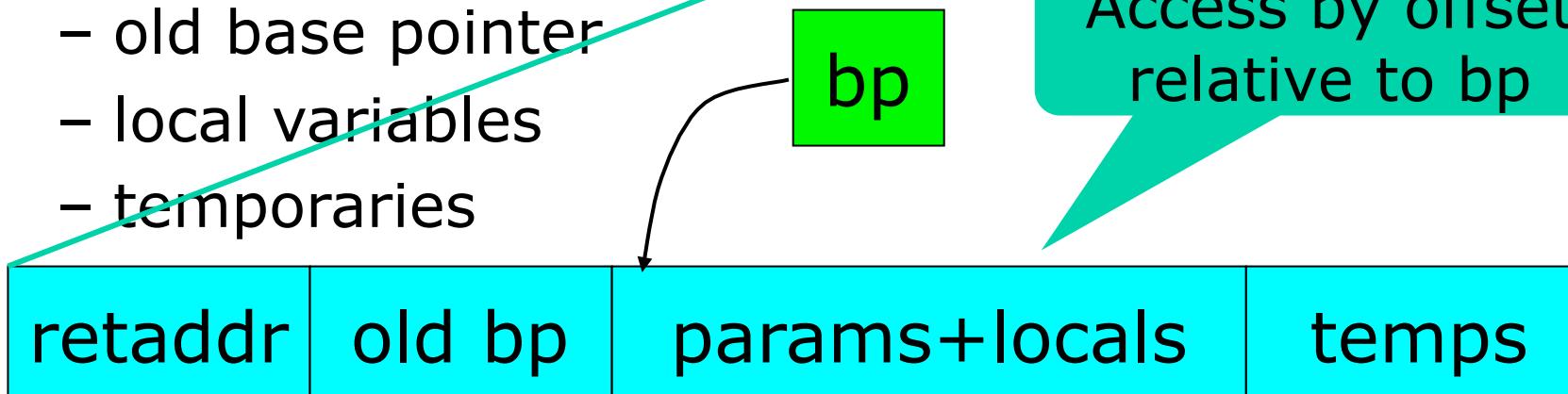


Runtime storage: the stack

- The store is an indexable stack
 - bottom: global variables at fixed addresses
 - followed by activation records



- An *activation record* is an executing function
 - return address
 - old base pointer
 - local variables
 - temporaries



Compiling micro-C

- Overall structure of a micro-C program
 - Global variable declarations `int x; int y;`
 - Global function declarations `void main(...)` `{...}`
- Overall structure of the generated code:
 - Code to allocate all global variables
 - Code to load arguments, call `main`, and stop
 - Code for each function, including `main`
- Structure of code for a function:
 - Code for the function's body statement
 - Code (RET) to return from the function



Observations

- At runtime, a local variable's place within a stack frame is always the same
- This *offset* can be computed at compile-time
- The compiletime environment in the micro-C compiler maps a local variable to an offset
- The runtime environment is the stack of activation records in the abstract machine
- At runtime, the base pointer BP points at the bottom of the current activation record
- So a local variable's address is $\text{BP}+\text{offset}$



Compile-time environments

- varEnv = variable environment
 - maps global variable to global address in stack
 - maps local variable to offset in activation record
- funEnv = function environment
 - maps function name to
(label, returntype, parametertypes)



Main micro-C compiler functions

- **cStmt stmt varEnv funEnv : instr list**
 - Compile **stmt** to code that performs the statement's actions
- **cExpr expr varEnv funEnv : instr list**
 - Compile **expr** to code that leaves the expr's rvalue on the stack top
- **cAccess expr varEnv funEnv : instr list**
 - Compile **expr** to code that leaves the expr's lvalue on the stack top
- **cProgram topdecs : instr list**
 - Build global varEnv and global funEnv
 - Generate code for global variables
 - Generate code to call function **main**
 - Generate code for all functions, including **main**



Compiling arithmetic expressions and assignment

- $\langle e1 \rangle$ means: the result of compiling $e1$

Compile 17 as rvalue:
CSTI 17

Compile $e1 + e2$ as rvalue:
 $\langle e1 \rangle$ as rvalue
 $\langle e2 \rangle$ as rvalue
ADD

Compile $e1 = e2$ as rvalue:
 $\langle e1 \rangle$ as lvalue
 $\langle e2 \rangle$ as rvalue
STI

cExpr



Micro-C compiler fragment

```
and cExpr e varEnv funEnv : instr list =
  match e with
  | Access acc      -> cAccess acc varEnv funEnv
                           @ [LDI]
  | Assign(acc, e)  -> cAccess acc varEnv funEnv
                           @ cExpr e varEnv funEnv
                           @ [STI]
  | CstI i          -> [CSTI i]
  | Addr acc        -> cAccess acc varEnv funEnv
  | Prim2(ope, e1, e2) ->
    cExpr e1 varEnv funEnv
    @ cExpr e2 varEnv funEnv
    @ (match ope with
       | "*"   -> [MUL]
       | "+"   -> [ADD]
       | "<"   -> [LT]
       | ... )
  | ...
```



Compiling comparisons

Compile $e1 < e2$ as rvalue:

$<e1>$ as rvalue

$<e2>$ as rvalue

LT

cExpr

- Q: How compile \geq , $>$, \leq when we have only LT?
- A: Use NOT and SWAP – but how?



Compiling lvalues and rvalues

Compile **x** as lvalue:

GETBP

CSTI <xoffset>

ADD

Compile **e** as rvalue:

<e> as lvalue

LDI

Compile **e1[e2]** as lvalue:

<e1> as rvalue

<e2> as rvalue

ADD

Compile **&e** as rvalue:

<e> as lvalue

Compile ***e** as lvalue:

<e> as rvalue

cAccess

cExpr



Compiling blocks and declarations

- To compile a block { **s₁ s₂ ... s_n** }
 - Make new scope in varEnv
 - Compile <s₁> <s₂> ... <s_n>
 - Drop new scope from varEnv
 - Generate code (INCSP (-m)) to forget m locals
- To compile int declaration **int x**
 - Generate code to increment stack pointer by 1
- To compile array declaration **int a[5]**
 - Generate code to allocate 5 stack places, that is, increment stack pointer by 5
 - Generate code to compute address of the first of those locations, and put it on the stack

Statement compilation schemes

Compile if (e) s1 else s2:

```
<e> as rvalue  
IFZERO L1  
<s1>  
GOTO L2  
L1: <s2>  
L2:
```

Compile while (e) s:

```
GOTO L2  
L1: <s>  
L2: <e> as rvalue  
IFNZRO L1
```

Compile e; :

```
<e> as rvalue  
INCSP -1
```

cStmt



Micro-C compiler fragment

```
let rec cStmt stmt varEnv funEnv : instr list =
  match stmt with
  | If(e, stmt1, stmt2) ->
    let labelse = newLabel()
    let labend = newLabel()
    in cExpr e varEnv funEnv @ [IFZERO labelse]
      @ cStmt stmt1 varEnv funEnv @ [GOTO labend]
      @ [Label labelse] @ cStmt stmt2 varEnv funEnv
      @ [Label labend]
  | While(e, body) ->
    let labbegin = newLabel()
    let labtest = newLabel()
    in [GOTO labtest; Label labbegin]
      @ cStmt body varEnv funEnv
      @ [Label labtest] @ cExpr e varEnv funEnv
      @ [IFNZRO labbegin]
  | Expr e -> cExpr e varEnv funEnv @ [INCSP -1]
  | ...
```



Ten-minute exercise

- What code should be generated for a **do-while** block:

```
do  
    stmt  
while (e) ;
```

- What code should be generated for a **for** statement:

```
for (e1; e2; e3)  
    stmt
```



Compiling and running Micro-C programs

```
fslex --unicode CLex.fsl  
fsyacc --module CPar CPar.fsy  
fsi -r FSharp.PowerPack.dll Absyn.fs CPar.fs \  
CLex.fs Parse.fs Machine.fs Comp.fs ParseAndComp.fs
```

Build compiler

```
open ParseAndComp;;  
compileToFile (fromFile "ex9.c") "ex9.out";;  
#q;;
```

Compile fac ex.

```
javac Machine.java
```

Compile stack
machine

```
java Machine ex9.out 8
```

Run it

```
java Machinetrace ex9.out 8
```

... with tracing



The code generated for ex9.c

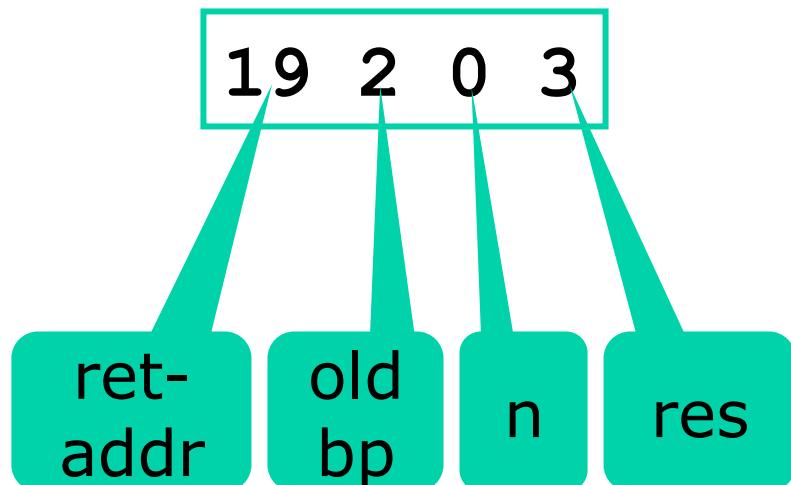
0 LDARGS	init	34 CSTI 0	68 ADD
1 CALL 1 L1		36 ADD	69 CALL 2 L2
4 STOP		37 LDI	72 INCSP -1
5 L1:		38 CSTI 0	74 GETBP
5 CSTI 0	main	40 EQ	75 CSTI 1
7 GETBP		41 IFZERO L3	77 ADD
8 CSTI 0		43 GETBP	78 LDI
10 ADD		44 CSTI 1	79 GETBP
11 LDI		46 ADD	80 CSTI 2
12 GETBP		47 LDI	82 ADD
13 CSTI 1		48 CSTI 1	83 LDI
15 ADD		50 STI	84 GETBP
16 CALL 2 L2		51 INCSP -1	85 CSTI 0
19 INCSP -1		53 GOTO L4	87 ADD
21 GETBP		55 L3:	88 LDI
22 CSTI 1		55 CSTI 0	89 MUL
24 ADD		57 GETBP	90 STI
25 LDI		58 CSTI 0	91 INCSP -1
26 PRINTI		60 ADD	93 INCSP -1
27 INCSP -1		61 LDI	95 L4:
29 INCSP -1		62 CSTI 1	95 INCSP 0
21 RET 0		64 SUB	97 RET 1
33 L2:		65 GETBP	
33 GETBP	fac	66 CSTI 2	

The code generated for ex9.c

```
0 LDARGS  
1 CALL 1 L1  
4 STOP ←  
5 L1:  
5 CSTI 0  
7 GETBP  
8 CSTI 0  
10 ADD  
11 LDI  
12 GETBP  
13 CSTI 1  
15 ADD  
16 CALL 2 L2  
19 INCSP -1 ←  
21 GETBP  
22 CSTI 1  
24 ADD  
25 LDI  
26 PRINTI  
27 INCSP -1  
29 INCSP -1  
31 RET 0 →  
33 L2: ←  
33 GETBP  
  
34 CSTI 0  
36 ADD  
37 LDI  
38 CSTI 0  
40 EQ  
41 IFZERO L3  
43 GETBP  
44 CSTI 1  
46 ADD  
47 LDI  
48 CSTI 1  
50 STI  
51 INCSP -1  
53 GOTO L4  
55 L3:  
55 CSTI 0  
57 GETBP  
58 CSTI 0  
60 ADD  
61 LDI  
62 CSTI 1  
64 SUB  
65 GETBP  
66 CSTI 2  
68 ADD  
69 CALL 2 L2  
72 INCSP -1 ←  
74 GETBP  
75 CSTI 1  
77 ADD  
78 LDI  
79 GETBP  
80 CSTI 2  
82 ADD  
83 LDI  
84 GETBP  
85 CSTI 0  
87 ADD  
88 LDI  
89 MUL  
90 STI  
91 INCSP -1  
93 INCSP -1  
95 L4: →  
95 INCSP 0  
97 RET 1
```

Running ex9.c on 0: The stack of frames

- Example ex9.c:
computing fac(0)
- Stack frame for fac(0):



- What stack frame?

4 -999 0 0

```
[ ]{0: LDARGS}
[ 0 ]{1: CALL 1 5}
[ 4 -999 0 ]{5: CSTI 0}
[ 4 -999 0 0 ]{7: GETBP}
[ 4 -999 0 0 2 ]{8: CSTI 0}
[ 4 -999 0 0 2 0 ]{10: ADD}
[ 4 -999 0 0 2 1 ]{11: LDI}
[ 4 -999 0 0 0 ]{12: GETBP}
[ 4 -999 0 0 0 2 ]{13: CSTI 1}
[ 4 -999 0 0 0 2 1 ]{15: ADD}
[ 4 -999 0 0 0 3 ]{16: CALL 2 33}
[ 4 -999 0 0 19 2 0 3 ]{33: GETBP}
[ 4 -999 0 0 19 2 0 3 6 ]{34: CSTI 0}
[ 4 -999 0 0 19 2 0 3 6 0 ]{36: ADD}
[ 4 -999 0 0 19 2 0 3 6 ]{37: LDI}
[ 4 -999 0 0 19 2 0 3 0 ]{38: CSTI 0}
[ 4 -999 0 0 19 2 0 3 0 0 ]{40: EQ}
[ 4 -999 0 0 19 2 0 3 1 ]{41: IFZERO 55}
[ 4 -999 0 0 19 2 0 3 1 ]{43: GETBP}
[ 4 -999 0 0 19 2 0 3 6 ]{44: CSTI 1}
[ 4 -999 0 0 19 2 0 3 6 1 ]{46: ADD}
[ 4 -999 0 0 19 2 0 3 7 ]{47: LDI}
[ 4 -999 0 0 19 2 0 3 3 ]{48: CSTI 1}
[ 4 -999 0 0 19 2 0 3 3 1 ]{50: STI}
[ 4 -999 0 1 19 2 0 3 1 ]{51: INCSP -1}
[ 4 -999 0 1 19 2 0 3 ]{53: GOTO 95}
[ 4 -999 0 1 19 2 0 3 ]{95: INCSP 0}
[ 4 -999 0 1 19 2 0 3 ]{97: RET 1}
[ 4 -999 0 1 3 ]{19: INCSP -1}
[ 4 -999 0 1 ]{21: GETBP}
[ 4 -999 0 1 2 ]{22: CSTI 1}
[ 4 -999 0 1 2 1 ]{24: ADD}
[ 4 -999 0 1 3 ]{25: LDI}
[ 4 -999 0 1 1 ]{26: PRINTI}
1 [ 4 -999 0 1 1 ]{27: INCSP -1}
[ 4 -999 0 1 ]{29: INCSP -1}
[ 4 -999 0 ]{31: RET 0}
[ 0 ]{4: STOP}
```

Highlights from computing fac(3)

```
[ ]{0: LDARGS}
[ 3 ]{1: CALL 1 5}
[ 4 -999 3 ]{5: CSTI 0}
[ 4 -999 3 0 ]{7: GETBP}
...
[ 4 -999 3 0 3 3 ]{16: CALL 2 33}
[ 4 -999 3 0 19 2 3 3 ]{33: GETBP}
...
[ 4 -999 3 0 19 2 3 3 0 2 8 ]{69: CALL 2 33}
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 ]{33: GETBP}
...
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 0 1 13 ]{69: CALL 2 33}
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 0 72 11 1 13 ]{33: GETBP}
...
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 0 72 11 1 13 0 0 18 ]{69: CALL 2 33}
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 0 72 11 1 13 0 72 16 0 18 ]{33: GETBP}
...
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 0 72 11 1 13 1 72 16 0 18 ]{97: RET 1}
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 0 72 11 1 13 1 18 ]{72: INCSP -1}
...
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 1 72 11 1 13 1 97: RET 1]
[ 4 -999 3 0 19 2 3 3 0 72 6 2 8 1 13 ]{72: INCSP -1}
...
[ 4 -999 3 0 19 2 3 3 2 72 6 2 8 ]{97: RET 1}
[ 4 -999 3 0 19 2 3 3 2 8 ]{72: INCSP -1}
...
[ 4 -999 3 6 19 2 3 3 ]{97: RET 1}
...
[ 4 -999 3 6 3 ]{25: LDI}
[ 4 -999 3 6 6 ]{26: PRINTI}
6 [ 4 -999 3 6 6 ]{27: INCSP -1}
[ 4 -999 3 6 ]{29: INCSP -1}
[ 4 -999 3 ]{31: RET 0}
[ 3 ]{4: STOP}
```

The diagram illustrates the stack state during the computation of fac(3). The stack grows downwards. Labels indicate the ret-address, old bp, n, and res. The stack state is shown as a series of memory locations, each containing a value and an offset. The ret-address is at the top of the stack. The old bp is at the previous frame boundary. The n parameter is being passed through the stack. The res variable is being returned from the stack.



Shortcomings of the compiler

- The compiler often generates inefficient code

GETBP
CSTI 0
ADD
LDI

could
be

GETBP
LDI

INCSP -1
INCSP -1

could
be

INCSP -2

- The compiler itself is inefficient, using (@) a lot:

```
| If(e, stmt1, stmt2) ->
  let labelse = newLabel()
  let labend  = newLabel()
  in cExpr e varEnv funEnv @ [IFZERO labelse]
    @ cStmt stmt1 varEnv funEnv @ [GOTO labend]
    @ [Label labelse] @ cStmt stmt2 varEnv funEnv
    @ [Label labend]
```

- Tail calls are not executed in constant space
- We fix these problems in course week 10

Adding a switch-statement to micro-C

- Exercise this week, add switch-statement:
 - each case has an int constant and a block
 - no fall-through, no **break**, no **default**

```
switch (month) {  
    case 2:  
        { days = 28; if (y%4==0) days = 29; }  
    case 3:  
        { days = 31; }  
    case 1:  
        { days = 31; }  
}
```

- May be compiled as a sequence of tests
- The abstract syntax may be as simple as this:

```
Switch of expr * (int * stmt) list
```



Reading and homework

- This week's lecture:
 - PLCSD chapter 8
 - Exercises 8.1, 8.3, 8.4, 8.5, 8.6
- Next week's lecture
 - The Java and C#/.NET virtual machines
 - Garbage collection techniques
 - PLCSD chapter 9 and 10
 - David Bacon: Realtime garbage collection

